

## Stefan-Boltzmann Lamp 1008523

### Instruction manual

02/24 NF/ALF/UD



#### 1. Safety instructions

The Stefan-Boltzmann lamp conforms to the safety stipulations for electrical measuring, control and laboratory instruments as specified in DIN EN 61010 part 1. It is intended for use in dry rooms suitable for the operation of electrical equipment.

Safe operation of the equipment can be assured as long as it is used as stipulated. However, safety cannot be guaranteed if the equipment is used incorrectly or handled without due care and attention.

**Caution:** When in operation, the lamp can become very hot. There is then a risk of burns if it is touched. This can also result in greasy residues being burned onto the lamp.

- Do not touch the lamp with your fingers.
- Allow the lamp to cool after the experiment has been completed.

**Note:**

Applying a voltage of more than 13 V to the terminals is likely to destroy the filament.

- Never apply a voltage higher than 13 V across the two 4-mm sockets.

## 2. Description

The Stefan-Boltzmann lamp is a high temperature source with a tungsten filament. It is designed to produce thermal radiation and for investigating how such radiation depends on the temperature. It can be used to confirm the Stefan-Boltzmann law, as stated in the following equation:

$$P = \varepsilon \cdot \sigma \cdot A \cdot T^4.$$

$P$  in this equation is the power radiated,  $T$  is the absolute temperature of the filament,  $A$  is the area of the filament's surface,  $\sigma$  is the Stefan-Boltzmann constant and  $\varepsilon$  is a dimensionless constant of a value between 0 and 1. The temperature of the lamp can be determined from the resistance of the filament.

The filament represents a good approximation of a point source of heat radiation and is thus highly suitable for investigating the inverse square law for heat radiation.

## 3. Equipment

1 Stefan Boltzmann Lamp

1 Stand Rod, 130 mm long

## 4. Technical data

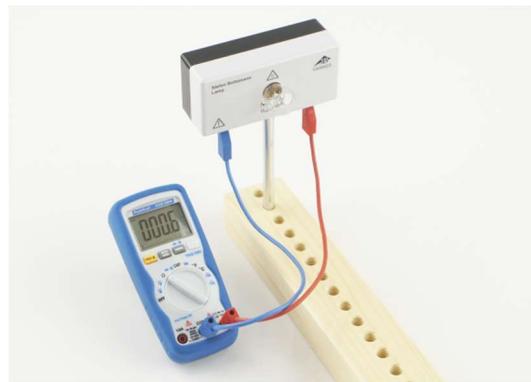
|                                  |              |
|----------------------------------|--------------|
| Nominal voltage:                 | 12 V DC      |
| Nominal current:                 | 1.75 A       |
| Nominal power:                   | 21 W         |
| Max. operating parameters:       | 13 V DC/ 2 A |
| Maximum temperature of filament: | 3600 K       |
| Distance of filament from rod:   | 25 mm        |

## 5. Sample measurements

Additionally required:

|  |         |
|--|---------|
| 1 Thermopile                               | 1000824 |
| 1 DC Power Supply, 20 V, 5 A (@230V)       | 1003312 |
| or   |         |
| 1 DC Power Supply, 20 V, 5 A (@115V)       | 1003311 |
| 1 Digital Multimeter P3340                 | 1002785 |
| 2 Digital Multimeters P1035                | 1002781 |
| 2 Barrel Feet, 1 kg                        | 1002834 |
| 1 Set of 15 Safety Experiment Leads, 75 cm | 1002843 |

### 5.1 Measurement of filament resistance at room temperature



- Insert one of the measuring leads into the COM socket of the digital multimeter P3340 (1002785) and one into its V  $\Omega$  mA socket, then short the leads together.
- Select the  $\Omega$  measuring range, wait for zero to be displayed and then briefly press the REL button.
- Break the contact between the leads and insert them into the sockets of the Stefan-Boltzmann lamp.
- Read off the resistance value  $R_{\text{ref}}$  and make a note of it (Tab. 1).
- Remove the measuring leads.
- Use the multimeter's temperature sensor to measure the ambient temperature  $T_{\text{ref}}$  in the vicinity of the lamp in Kelvin and make a note of it (Tab. 1).

Tab. 1: Value of filament resistance measured at room temperature

|                  |                |
|------------------|----------------|
| $R_{\text{ref}}$ | 0.541 $\Omega$ |
| $T_{\text{ref}}$ | 297 K          |

## 5.2 Measurement of radiant intensity as a function of the temperature of the filament



- Connect the thermopile to the P3340 digital multimeter (1002785).
- Set up the Stefan-Boltzmann lamp in front of the thermopile and connect up the DC power supply and the two P1035 digital multimeters (1002781).
- Apply a voltage in steps of 1 V up to a maximum of 12 V, measure the lamp voltage  $U$ , the lamp current  $I$ , and use the thermopile to measure the radiant intensity  $\Phi$  (5.3, Tab. 2).

## 5.3 Evaluation

- Calculate  $R = U/I$  (Tab. 2).
- Now the values determined,  $T_{\text{ref}}$ ,  $R_{\text{ref}}$ ,  $R$ , can be used along with the temperature coefficient of resistance for tungsten  $\alpha = 4.4 \cdot 10^{-3} \text{ K}^{-1}$  to calculate the temperature of the filament by means of the following formula (Tab. 2):

$$T = \left( \frac{R - R_{\text{ref}}}{\alpha \cdot R_{\text{ref}}} \right) + T_{\text{ref}}$$

One possible alternative method for determining the temperature  $T$  of the filament is to calculate the quotients  $R/R_{\text{ref}}$  and then use Fig. 2 or Tab. 3 to find the temperature.

**Note:** In Table 3 the quotient  $R/R_{\text{ref}}$  is specified for  $T_{\text{ref}} = 300 \text{ K}$  and for  $T_{\text{ref}} = 290 \text{ K}$ . It is possible to determine the temperature more precisely by interpolating between these two reference values to take account of the actual room temperature.

- Plot  $\Phi$  as a function of  $T^4$  (Fig. 3).

Tab. 2: Values for the resistance  $R$  and the temperature  $T$  of the filament calculated from the measured values for the lamp voltage  $U$  and the lamp current  $I$ , as well as the radiated intensity  $\Phi$  measured with the thermopile

| $U / \text{V}$ | $I / \text{A}$ | $R / \Omega$ | $T / \text{K}$ | $\Phi / \text{W}$ |
|----------------|----------------|--------------|----------------|-------------------|
| 0.00369        | 0.006          | 0.615        | 328            | 0                 |
| 1.0502         | 0.554          | 1.896        | 854            | 0.0001            |
| 2.033          | 0.706          | 2.879        | 1259           | 0.0004            |
| 3.012          | 0.837          | 3.599        | 1554           | 0.0011            |
| 4.003          | 0.958          | 4.178        | 1792           | 0.0019            |
| 5.012          | 1.071          | 4.679        | 1998           | 0.0029            |
| 6.017          | 1.174          | 5.125        | 2181           | 0.0042            |
| 7.074          | 1.276          | 5.5434       | 2353           | 0.0058            |
| 8.028          | 1.362          | 5.894        | 2497           | 0.0072            |
| 9.011          | 1.446          | 6.232        | 2636           | 0.0088            |
| 10.088         | 1.534          | 6.576        | 2777           | 0.0106            |
| 11.02          | 1.607          | 6.8575       | 2893           | 0.0125            |
| 11.685         | 1.68           | 6.955        | 2933           | 0.0145            |

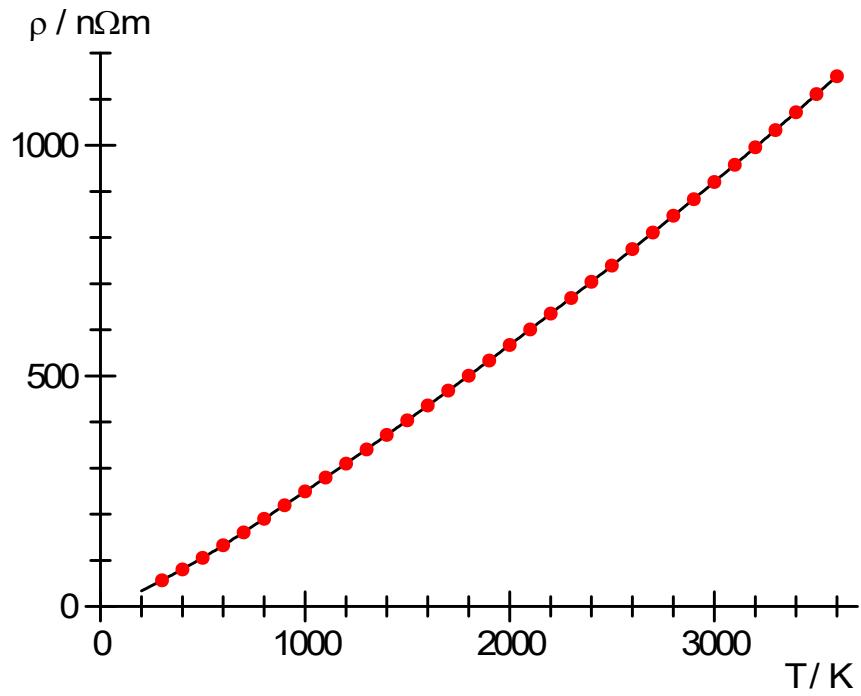


Fig. 1: Electrical resistivity  $\rho$  of tungsten as a function of absolute temperature  $T$  (see Tab. 3). Curve based on measurements made by Zerda, T.W., Texas Christian University, 2001

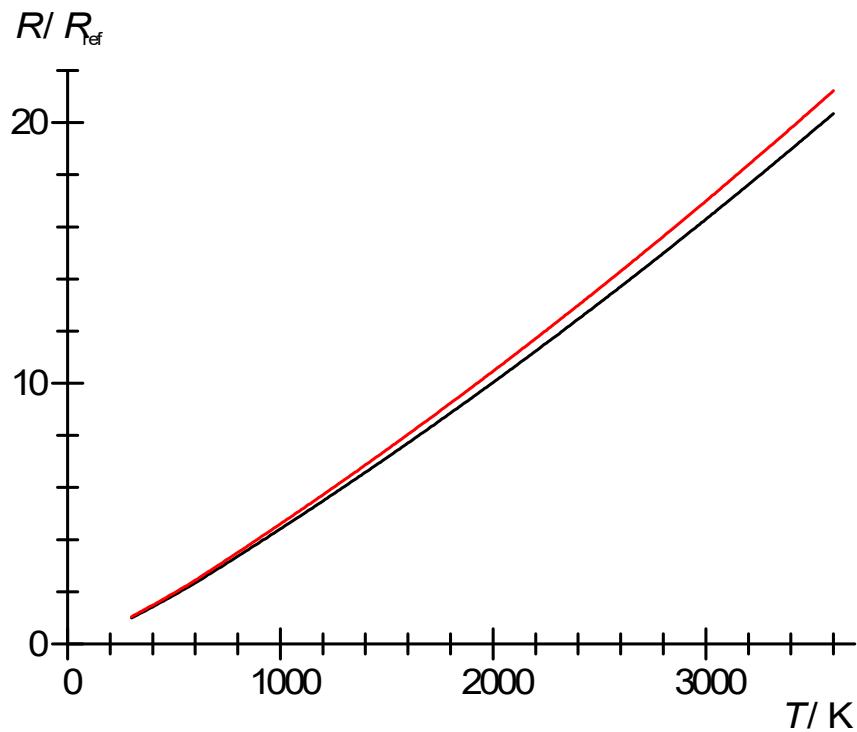


Fig. 2: Resistances ratios  $R(T)/R_{300 \text{ K}}$  (black) and  $R(T)/R_{290}$  (red) calculated from the values shown in Fig. 1 (see Tab. 3)

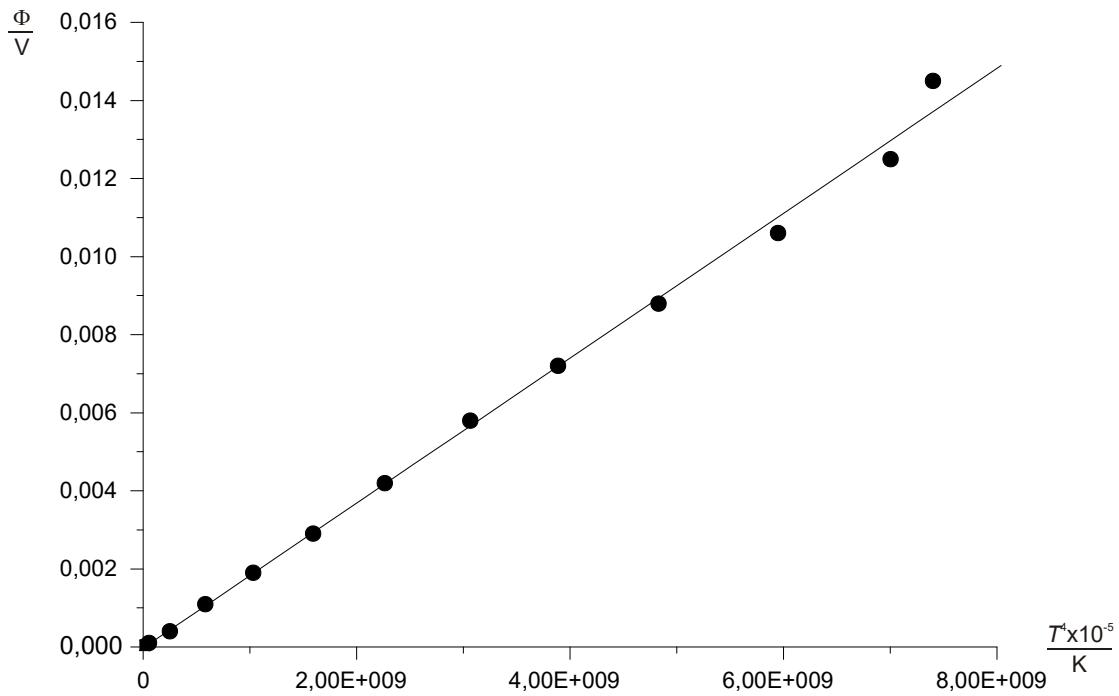


Fig. 3: Radiant intensity  $\Phi$  as a function of temperature  $T$

## 6. Changing bulbs

In order to change the bulb, the following equipment is also required:

1 Bulb, 12 V/21 W, socket BA15S

1 Screwdriver

1 Piece of sandpaper

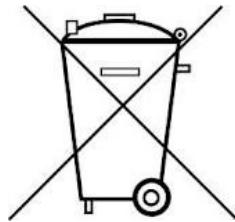
1 Soldering iron

Solder

- Unscrew the back of the housing.
- Unsolder the bulb.
- Sand down the contact surfaces where the wires are to be soldered to the new bulb and tin them with solder.
- Set the bulb in position and solder it in place.
- Test the lamp by applying a voltage of 12 V.
- Screw the housing back together.

## 7. Disposal

- Packaging should be disposed of at local recycling centres.
- Should the equipment need to be scrapped, it must not be disposed of in normal household waste. Local regulations for the disposal of electrical equipment should be observed.



## 8. Appendix

Tab. 3: Specific resistance  $\rho$  of tungsten as a function of the absolute temperature  $T$  and calculated resistance ratios  $R(T)/R_{300K}$  or  $R(T)/R_{290K}$  (see Fig. 1 and Fig. 2)

| $T$<br>K | $\rho$<br>nΩm | $R(T)$     |            | $R(T)$     |            | $T$<br>K | $\rho$<br>nΩm | $R(T)$     |            | $R(T)$     |            | $T$<br>K | $\rho$<br>nΩm | $R(T)$     |            | $R(T)$     |            |
|----------|---------------|------------|------------|------------|------------|----------|---------------|------------|------------|------------|------------|----------|---------------|------------|------------|------------|------------|
|          |               | $R_{300K}$ | $R_{290K}$ | $R_{300K}$ | $R_{290K}$ |          |               | $R_{300K}$ | $R_{290K}$ | $R_{300K}$ | $R_{290K}$ |          |               | $R_{300K}$ | $R_{290K}$ | $R_{300K}$ | $R_{290K}$ |
| 290      | 54.17         | 1.000      |            | 710        | 163.86     | 2.900    | 3.025         | 1130       | 288.49     | 5.106      | 5.325      | 1550     | 419.46        | 7.424      | 7.743      |            |            |
| 300      | 56.50         | 1.000      | 1.043      | 720        | 166.76     | 2.951    | 3.078         | 1140       | 291.53     | 5.160      | 5.381      | 1560     | 422.65        | 7.481      | 7.802      |            |            |
| 310      | 58.84         | 1.041      | 1.086      | 730        | 169.65     | 3.003    | 3.132         | 1150       | 294.58     | 5.214      | 5.438      | 1570     | 425.85        | 7.537      | 7.861      |            |            |
| 320      | 61.19         | 1.083      | 1.130      | 740        | 172.55     | 3.054    | 3.185         | 1160       | 297.63     | 5.268      | 5.494      | 1580     | 429.06        | 7.594      | 7.920      |            |            |

|     |        |       |       |      |        |       |       |      |        |       |       |      |        |       |        |
|-----|--------|-------|-------|------|--------|-------|-------|------|--------|-------|-------|------|--------|-------|--------|
| 330 | 63.56  | 1.125 | 1.173 | 750  | 175.46 | 3.105 | 3.239 | 1170 | 300.69 | 5.322 | 5.550 | 1590 | 432.26 | 7.651 | 7.979  |
| 340 | 65.93  | 1.167 | 1.217 | 760  | 178.37 | 3.157 | 3.292 | 1180 | 303.75 | 5.376 | 5.607 | 1600 | 435.47 | 7.707 | 8.038  |
| 350 | 68.33  | 1.209 | 1.261 | 770  | 181.28 | 3.208 | 3.346 | 1190 | 306.81 | 5.430 | 5.663 | 1610 | 438.69 | 7.764 | 8.098  |
| 360 | 70.73  | 1.252 | 1.306 | 780  | 184.19 | 3.260 | 3.400 | 1200 | 309.87 | 5.484 | 5.720 | 1620 | 441.90 | 7.821 | 8.157  |
| 370 | 73.14  | 1.295 | 1.350 | 790  | 187.11 | 3.312 | 3.454 | 1210 | 312.94 | 5.539 | 5.777 | 1630 | 445.13 | 7.878 | 8.217  |
| 380 | 75.57  | 1.338 | 1.395 | 800  | 190.03 | 3.363 | 3.508 | 1220 | 316.02 | 5.593 | 5.833 | 1640 | 448.35 | 7.935 | 8.276  |
| 390 | 78.02  | 1.381 | 1.440 | 810  | 192.96 | 3.415 | 3.562 | 1230 | 319.09 | 5.648 | 5.890 | 1650 | 451.58 | 7.992 | 8.336  |
| 400 | 80.47  | 1.424 | 1.485 | 820  | 195.89 | 3.467 | 3.616 | 1240 | 322.18 | 5.702 | 5.947 | 1660 | 454.81 | 8.050 | 8.395  |
| 410 | 82.94  | 1.468 | 1.531 | 830  | 198.82 | 3.519 | 3.670 | 1250 | 325.26 | 5.757 | 6.004 | 1670 | 458.05 | 8.107 | 8.455  |
| 420 | 85.42  | 1.512 | 1.577 | 840  | 201.76 | 3.571 | 3.724 | 1260 | 328.35 | 5.811 | 6.061 | 1680 | 461.28 | 8.164 | 8.515  |
| 430 | 87.91  | 1.556 | 1.623 | 850  | 204.70 | 3.623 | 3.779 | 1270 | 331.44 | 5.866 | 6.118 | 1690 | 464.53 | 8.222 | 8.575  |
| 440 | 90.42  | 1.600 | 1.669 | 860  | 207.64 | 3.675 | 3.833 | 1280 | 334.53 | 5.921 | 6.175 | 1700 | 467.77 | 8.279 | 8.635  |
| 450 | 92.94  | 1.645 | 1.716 | 870  | 210.59 | 3.727 | 3.887 | 1290 | 337.63 | 5.976 | 6.232 | 1710 | 471.02 | 8.337 | 8.695  |
| 460 | 95.47  | 1.690 | 1.762 | 880  | 213.54 | 3.779 | 3.942 | 1300 | 340.73 | 6.031 | 6.290 | 1720 | 474.28 | 8.394 | 8.755  |
| 470 | 98.02  | 1.735 | 1.809 | 890  | 216.50 | 3.832 | 3.996 | 1310 | 343.84 | 6.086 | 6.347 | 1730 | 477.53 | 8.452 | 8.815  |
| 480 | 100.57 | 1.780 | 1.857 | 900  | 219.45 | 3.884 | 4.051 | 1320 | 346.95 | 6.141 | 6.404 | 1740 | 480.79 | 8.510 | 8.875  |
| 490 | 103.15 | 1.826 | 1.904 | 910  | 222.42 | 3.937 | 4.106 | 1330 | 350.06 | 6.196 | 6.462 | 1750 | 484.06 | 8.567 | 8.935  |
| 500 | 105.73 | 1.871 | 1.952 | 920  | 225.38 | 3.989 | 4.160 | 1340 | 353.18 | 6.251 | 6.519 | 1760 | 487.33 | 8.625 | 8.996  |
| 510 | 108.33 | 1.917 | 2.000 | 930  | 228.35 | 4.042 | 4.215 | 1350 | 356.30 | 6.306 | 6.577 | 1770 | 490.60 | 8.683 | 9.056  |
| 520 | 110.93 | 1.963 | 2.048 | 940  | 231.32 | 4.094 | 4.270 | 1360 | 359.42 | 6.361 | 6.635 | 1780 | 493.87 | 8.741 | 9.116  |
| 530 | 113.56 | 2.010 | 2.096 | 950  | 234.30 | 4.147 | 4.325 | 1370 | 362.55 | 6.417 | 6.692 | 1790 | 497.15 | 8.799 | 9.177  |
| 540 | 116.19 | 2.056 | 2.145 | 960  | 237.28 | 4.200 | 4.380 | 1380 | 365.68 | 6.472 | 6.750 | 1800 | 500.43 | 8.857 | 9.238  |
| 550 | 118.84 | 2.103 | 2.194 | 970  | 240.26 | 4.252 | 4.435 | 1390 | 368.82 | 6.528 | 6.808 | 1810 | 503.72 | 8.915 | 9.298  |
| 560 | 121.50 | 2.150 | 2.243 | 980  | 243.25 | 4.305 | 4.490 | 1400 | 371.95 | 6.583 | 6.866 | 1820 | 507.01 | 8.974 | 9.359  |
| 570 | 124.17 | 2.198 | 2.292 | 990  | 246.24 | 4.358 | 4.545 | 1410 | 375.10 | 6.639 | 6.924 | 1830 | 510.30 | 9.032 | 9.420  |
| 580 | 126.86 | 2.245 | 2.342 | 1000 | 249.23 | 4.411 | 4.601 | 1420 | 378.24 | 6.695 | 6.982 | 1840 | 513.60 | 9.090 | 9.481  |
| 590 | 129.56 | 2.293 | 2.392 | 1010 | 252.23 | 4.464 | 4.656 | 1430 | 381.39 | 6.750 | 7.040 | 1850 | 516.90 | 9.149 | 9.541  |
| 600 | 132.27 | 2.341 | 2.442 | 1020 | 255.23 | 4.517 | 4.711 | 1440 | 384.54 | 6.806 | 7.098 | 1860 | 520.20 | 9.207 | 9.602  |
| 610 | 135.13 | 2.392 | 2.494 | 1030 | 258.24 | 4.571 | 4.767 | 1450 | 387.70 | 6.862 | 7.157 | 1870 | 523.51 | 9.266 | 9.663  |
| 620 | 137.98 | 2.442 | 2.547 | 1040 | 261.25 | 4.624 | 4.822 | 1460 | 390.86 | 6.918 | 7.215 | 1880 | 526.82 | 9.324 | 9.725  |
| 630 | 140.85 | 2.493 | 2.600 | 1050 | 264.26 | 4.677 | 4.878 | 1470 | 394.02 | 6.974 | 7.273 | 1890 | 530.13 | 9.383 | 9.786  |
| 640 | 143.71 | 2.544 | 2.653 | 1060 | 267.28 | 4.731 | 4.934 | 1480 | 397.19 | 7.030 | 7.332 | 1900 | 533.45 | 9.442 | 9.847  |
| 650 | 146.58 | 2.594 | 2.706 | 1070 | 270.29 | 4.784 | 4.989 | 1490 | 400.36 | 7.086 | 7.390 | 1910 | 536.77 | 9.500 | 9.908  |
| 660 | 149.45 | 2.645 | 2.759 | 1080 | 273.32 | 4.837 | 5.045 | 1500 | 403.53 | 7.142 | 7.449 | 1920 | 540.10 | 9.559 | 9.970  |
| 670 | 152.33 | 2.696 | 2.812 | 1090 | 276.34 | 4.891 | 5.101 | 1510 | 406.71 | 7.198 | 7.508 | 1930 | 543.43 | 9.618 | 10.031 |
| 680 | 155.20 | 2.747 | 2.865 | 1100 | 279.37 | 4.945 | 5.157 | 1520 | 409.89 | 7.255 | 7.566 | 1940 | 546.76 | 9.677 | 10.093 |
| 690 | 158.09 | 2.798 | 2.918 | 1110 | 282.41 | 4.998 | 5.213 | 1530 | 413.08 | 7.311 | 7.625 | 1950 | 550.10 | 9.736 | 10.154 |
| 700 | 160.97 | 2.849 | 2.971 | 1120 | 285.45 | 5.052 | 5.269 | 1540 | 416.27 | 7.368 | 7.684 | 1960 | 553.44 | 9.795 | 10.216 |

| $T$  | $\rho$ | $R(T)$     | $R(T)$     |
|------|--------|------------|------------|------|--------|------------|------------|------|--------|------------|------------|------|--------|------------|------------|
| K    | nΩm    | $R_{300K}$ | $R_{290K}$ |
| 1970 | 556.78 | 9.854      | 10.278     | 2380 | 696.95 | 12.335     | 12.865     | 2790 | 843.18 | 14.923     | 15.564     | 3200 | 995.45 | 17.618     | 18.375     |
| 1980 | 560.13 | 9.914      | 10.339     | 2390 | 700.45 | 12.397     | 12.930     | 2800 | 846.82 | 14.988     | 15.631     | 3210 | 999.24 | 17.686     | 18.445     |
| 1990 | 563.48 | 9.973      | 10.401     | 2400 | 703.95 | 12.459     | 12.994     | 2810 | 850.46 | 15.052     | 15.699     | 3220 | 1003.0 | 17.753     | 18.515     |
| 2000 | 566.83 | 10.032     | 10.463     | 2410 | 707.45 | 12.521     | 13.059     | 2820 | 854.11 | 15.117     | 15.766     | 3230 | 1006.8 | 17.820     | 18.585     |
| 2010 | 570.19 | 10.092     | 10.525     | 2420 | 710.95 | 12.583     | 13.124     | 2830 | 857.77 | 15.182     | 15.834     | 3240 | 1010.6 | 17.887     | 18.655     |
| 2020 | 573.55 | 10.151     | 10.587     | 2430 | 714.46 | 12.645     | 13.188     | 2840 | 861.42 | 15.246     | 15.901     | 3250 | 1014.4 | 17.954     | 18.725     |
| 2030 | 576.91 | 10.211     | 10.649     | 2440 | 717.97 | 12.707     | 13.253     | 2850 | 865.08 | 15.311     | 15.969     | 3260 | 1018.2 | 18.022     | 18.796     |
| 2040 | 580.28 | 10.270     | 10.711     | 2450 | 721.49 | 12.770     | 13.318     | 2860 | 868.75 | 15.376     | 16.036     | 3270 | 1022.1 | 18.089     | 18.866     |
| 2050 | 583.65 | 10.330     | 10.774     | 2460 | 725.01 | 12.832     | 13.383     | 2870 | 872.41 | 15.441     | 16.104     | 3280 | 1025.9 | 18.157     | 18.937     |
| 2060 | 587.03 | 10.390     | 10.836     | 2470 | 728.53 | 12.894     | 13.448     | 2880 | 876.08 | 15.506     | 16.172     | 3290 | 1029.7 | 18.224     | 19.007     |
| 2070 | 590.41 | 10.450     | 10.898     | 2480 | 732.06 | 12.957     | 13.513     | 2890 | 879.76 | 15.571     | 16.240     | 3300 | 1033.5 | 18.292     | 19.078     |
| 2080 | 593.79 | 10.510     | 10.961     | 2490 | 735.59 | 13.019     | 13.578     | 2900 | 883.44 | 15.636     | 16.307     | 3310 | 1037.3 | 18.360     | 19.148     |
| 2090 | 597.18 | 10.569     | 11.023     | 2500 | 739.12 | 13.082     | 13.644     | 2910 | 887.12 | 15.701     | 16.375     | 3320 | 1041.2 | 18.428     | 19.219     |
| 2100 | 600.57 | 10.629     | 11.086     | 2510 | 742.66 | 13.144     | 13.709     | 2920 | 890.80 | 15.766     | 16.443     | 3330 | 1045.0 | 18.495     | 19.290     |
| 2110 | 603.96 | 10.690     | 11.149     | 2520 | 746.20 | 13.207     | 13.774     | 2930 | 894.49 | 15.832     | 16.511     | 3340 | 1048.8 | 18.563     | 19.360     |
| 2120 | 607.36 | 10.750     | 11.211     | 2530 | 749.75 | 13.270     | 13.840     | 2940 | 898.18 | 15.897     | 16.580     | 3350 | 1052.7 | 18.631     | 19.431     |
| 2130 | 610.76 | 10.810     | 11.274     | 2540 | 753.30 | 13.333     | 13.905     | 2950 | 901.88 | 15.962     | 16.648     | 3360 | 1056.5 | 18.699     | 19.502     |
| 2140 | 614.17 | 10.870     | 11.337     | 2550 | 756.85 | 13.395     | 13.971     | 2960 | 905.58 | 16.028     | 16.716     | 3370 | 1060.4 | 18.767     | 19.573     |
| 2150 | 617.57 | 10.930     | 11.400     | 2560 | 760.40 | 13.458     | 14.036     | 2970 | 909.28 | 16.093     | 16.785     | 3380 | 1064.2 | 18.836     | 19.644     |
| 2160 | 620.99 | 10.991     | 11.463     | 2570 | 763.96 | 13.521     | 14.102     | 2980 | 912.99 | 16.159     | 16.853     | 3390 | 1068.1 | 18.904     | 19.716     |
| 2170 | 624.40 | 11.051     | 11.526     | 2580 | 767.53 | 13.584     | 14.168     | 2990 | 916.70 | 16.225     | 16.921     | 3400 | 1071.9 | 18.972     | 19.787     |
| 2180 | 627.82 | 11.112     | 11.589     | 2590 | 771.09 | 13.648     | 14.234     | 3000 | 920.41 | 16.290     | 16.990     | 3410 | 1075.8 | 19.040     | 19.858     |
| 2190 | 631.24 | 11.172     | 11.652     | 2600 | 774.66 | 13.711     | 14.300     | 3010 | 924.13 | 16.356     | 17.059     | 3420 | 1079.7 | 19.109     | 19.929     |
| 2200 | 634.67 | 11.233     | 11.715     | 2610 | 778.24 | 13.774     | 14.366     | 3020 | 927.85 | 16.422     | 17.127     | 3430 | 1083.5 | 19.177     | 20.001     |
| 2210 | 638.10 | 11.294     | 11.779     | 2620 | 781.81 | 13.837     | 14.432     | 3030 | 931.58 | 16.488     | 17.196     | 3440 | 1087.4 | 19.246     | 20.072     |
| 2220 | 641.53 | 11.354     | 11.842     | 2630 | 785.39 | 13.901     | 14.498     | 3040 | 935.31 | 16.554     | 17.265     | 3450 | 1091.3 | 19.314     | 20.144     |
| 2230 | 644.97 | 11.415     | 11.906     | 2640 | 788.98 | 13.964     | 14.564     | 3050 | 939.04 | 16.620     | 17.334     | 3460 | 1095.2 | 19.383     | 20.215     |
| 2240 | 648.41 | 11.476     | 11.969     | 2650 | 792.57 | 14.028     | 14.630     | 3060 | 942.77 | 16.686     | 17.403     | 3470 | 1099.0 | 19.452     | 20.287     |
| 2250 | 651.85 | 11.537     | 12.033     | 2660 | 796.16 | 14.091     | 14.696     | 3070 | 946.51 | 16.752     | 17.472     | 3480 | 1102.9 | 19.521     | 20.359     |
| 2260 | 655.30 | 11.598     | 12.096     | 2670 | 799.75 | 14.155     | 14.763     | 3080 | 950.26 | 16.819     | 17.541     | 3490 | 1106.8 | 19.589     | 20.431     |
| 2270 | 658.75 | 11.659     | 12.160     | 2680 | 803.35 | 14.219     | 14.829     | 3090 | 954.00 | 16.885     | 17.610     | 3500 | 1110.7 | 19.658     | 20.503     |
| 2280 | 662.21 | 11.720     | 12.224     | 2690 | 806.95 | 14.282     | 14.896     | 3100 | 957.75 | 16.951     | 17.679     | 3510 | 1114.6 | 19.727     | 20.574     |
| 2290 | 665.66 | 11.782     | 12.288     | 2700 | 810.56 | 14.346     | 14.962     | 3110 | 961.51 | 17.018     | 17.748     | 3520 | 1118.5 | 19.796     | 20.646     |
| 2300 | 669.13 | 11.843     | 12.351     | 2710 | 814.17 | 14.410     | 15.029     | 3120 | 965.26 | 17.084     | 17.818     | 3530 | 1122.4 | 19.865     | 20.719     |
| 2310 | 672.59 | 11.904     | 12.415     | 2720 | 817.78 | 14.474     | 15.096     | 3130 | 969.02 | 17.151     | 17.887     | 3540 | 1126.3 | 19.935     | 20.791     |
| 2320 | 676.06 | 11.966     | 12.479     | 2730 | 821.40 | 14.538     | 15.162     | 3140 | 972.79 | 17.217     | 17.957     | 3550 | 1130.2 | 20.004     | 20.863     |
| 2330 | 679.53 | 12.027     | 12.544     | 2740 | 825.02 | 14.602     | 15.229     | 3150 | 976.56 | 17.284     | 18.026     | 3560 | 1134.1 | 20.073     | 20.935     |
| 2340 | 683.01 | 12.089     | 12.608     | 2750 | 828.64 | 14.666     | 15.296     | 3160 | 980.33 | 17.351     | 18.096     | 3570 | 1138.1 | 20.143     | 21.008     |
| 2350 | 686.49 | 12.150     | 12.672     | 2760 | 832.27 | 14.730     | 15.363     | 3170 | 984.10 | 17.418     | 18.166     | 3580 | 1142.0 | 20.212     | 21.080     |
| 2360 | 689.97 | 12.212     | 12.736     | 2770 | 835.90 | 14.795     | 15.430     | 3180 | 987.88 | 17.485     | 18.235     | 3590 | 1145.9 | 20.281     | 21.152     |
| 2370 | 693.46 | 12.274     | 12.801     | 2780 | 839.54 | 14.859     | 15.497     | 3190 | 991.66 | 17.551     | 18.305     | 3600 | 1149.8 | 20.351     | 21.225     |